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## Artificial Intelligence

### – Sheet 1: Agents and Problem Formulation –

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Date: 06. April 2011

Remarks:

- Exercises can be solved in **groups up to 2 students**.
- With **formal proofs** we do really mean **formal proofs**; i.e., not just text but mathematical methods (e.g. *proofs by induction*, proper formalizations, etc.).
- In order to be **permitted to the exam**, Clausthal students must have fulfilled the following requirement: In **average 50%** of each exercise sheet has to be solved successfully *and* on all but one exercise sheet at least **25%** of the points have to be reached.

Points:

\_\_\_\_\_ of 20

Group / Tutor:

#### Exercise 1 (2 Points, Performance vs. utility)

Both the performance measure and the utility function evaluate how well an agent is doing. Explain the **difference** with *a few* sentences.

Name(s) & Matr. no.:

#### Exercise 2 (6 Points, Expressiveness of standard agents)

Give **formal** proofs of the following claims.

1. For every purely reactive agent, there is a behaviorally equivalent standard agent.
2. There are standard agents that have no behaviorally equivalent purely reactive agent.

#### Exercise 3 (4 Points, Equivalence of agents)

**Formally** prove Theorem 1.18: State-based agents are equivalent in expressive power to standard agents, i.e. that for every state-based agent there is a behaviorally equivalent standard agent *and* vice versa.

To be submitted:

20. April 2011  
before class

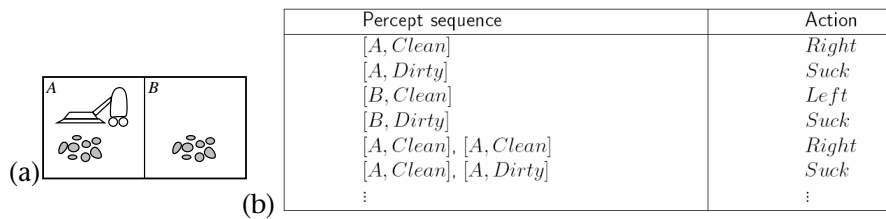


Figure 1: Vacuum-world

### Exercise 4 (4 Points, Rational agents)

Consider the following definition of a *rational agent*:

For each possible percept sequence  $per$ , a rational agent should select an action that is expected to maximize its performance measure, given the evidence provided by  $per$  and whatever built-in knowledge the agent has.

Now consider the following scenario. There are two rooms  $A$  and  $B$ , each can be *dirty* or *clean* (cf. Figure 1(a)). A vacuum-cleaner agent can perform actions *left*, *right*, and *suck* (all actions have their obvious effects). Actions may fail with some low probability.

Does the the simple agent program in Figure 1(b) describe a rational agent? Show formal arguments for both possible answers.

### Exercise 5 (4 Points, Problem formulation)

Suppose that  $\text{Successor-Fn}(s)$  consists of all tuples  $(a, s')$  such that  $s'$  is reachable by  $s$  if  $a$  is performed,  $\text{Legal-Action}(s)$  denotes the set of actions that are legal in state  $s$ , and  $\text{Result}(a, s)$  denotes the states that result from performing legal action  $a$  in state  $s$ .

Define each of these notions as **a function of the other two** (i.e, for instance,  $\text{Successor-Fn}$  in terms of  $\text{Legal-Actions}$  and  $\text{Result}$ ).